Subject: VCE (Mathematical Methods) Unit: 3 Week **Area of Study Learning Focus** Term 4 Headstart Functions and Relations: 1A - 1H, 2A, 2B Investigate concepts of relations and functions, domain, implied (maximal) domain, restrictions and range. Investigate and sketch graphs for odd and even functions, one-to-one and inverse functions, sums and products and addition of ordinates. Define and use composite functions, strictly increasing and decreasing functions and power functions and their graphs. Apply a knowledge of functions to solve problems. Term 1 Coordinate Geometry and Matrices: 2C – 2G, 3A, 3B. **Functions and Graphs** 1-3 Solving linear and literal equations, simultaneous linear equations with Algebra two or more variables and interpret the geometry Find the distance between two points, midpoint of a line segment and gradient of a straight line. Recognise different forms of the equation of a straight line and use matrices. Apply a knowledge of linear functions to solve problems. 4-5 **Functions and Graphs** Transformations: 3C - 3I Use notation for translations, reflections in an axis and dilations from an Algebra axis and determine sequences of transformations given an original and image equation, and use them to sketch graphs. Consider transformations of power functions. Determine function rules from transformations and graphs. Use matrices to define transformations and determine images. 6 **Functions and Graphs** Polynomial Functions: 3J, 4A -4F Revise properties of quadratic functions and consider properties of Algebra cubic functions and polynomials of higher degree. Add, subtract, multiply and divide polynomials, equate coefficients and use sign diagrams. Use the language of polynomials, the remainder theorem, factor theorem and the rational-root theorem and identify the linear factors of cubic and quartic polynomials. Determine the rules for given polynomial graphs and apply polynomial functions to problem solving. 7 **Functions and Graphs** Exponential and Logarithmic Functions: 4G – 4H, 5A - 5E Graph exponential and logarithmic functions and their transformations. Algebra Revise the index and logarithm laws and solve exponential and logarithmic equations. Determine rules for graphing exponential and logarithmic functions and find their inverses. Apply exponential functions to modelling growth and decay. 8-9 **Functions and Graphs** Circular Functions: 5F -5I, 6A-6C Circular Function Graphing: 6D - 6L Algebra Define the sine, cosine and tangent circular functions, explore their symmetry properties, apply the Pythagorean Identity, find exact values and sketch graphs of circular functions and their transformations. Measure angles in degrees and radians, solve equations and apply circular functions in modelling periodic motion. Use addition of ordinates, determine rules for graphing and find general solutions of trigonometric equations Apply circular functions to problem solving 10 Further Functions: 7A-7E **Functions and Graphs** Graph power functions with rational non-integer index. Algebra

		Revisit sums, differences and products of functions, addition of
	Calculus	<ul> <li>Revisit stiffs, differences and products of functions, addition of ordinates, one-to-one functions, strictly increasing and decreasing functions, odd functions and even functions, composite functions, inverse functions and transformations of functions.</li> <li>Use functional equations to describe properties of functions.</li> <li>Use parameters to describe families of functions.</li> <li>Differentiation: 9A-9C</li> <li>Understand limits, the definition of differentiation and the notation for the derivative of a polynomial function.</li> <li>Find the gradient of a tangent to the graph of a polynomial function by calculating its derivative.</li> </ul>
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Term 2 1-3	Calculus	<ul> <li>Differentiation continued: 9D-9M</li> <li>Understand and use the chain, product and quotient rules</li> <li>Differentiate rational powers, exponential, natural logarithmic and circular functions.</li> <li>Deduce the graph of the derivative from the graph of a function and vice versa, determine continuity and differentiability</li> </ul>
4-5	Calculus	<ul> <li>Applications of Differentiation: 10A – 10G</li> <li>Find the equations of the tangent and the normal at a given point.</li> <li>Find stationary points and state their nature.</li> <li>Use differentiation techniques to sketch graphs and show families of functions</li> <li>Solve maximum and minimum problems, determine absolute maximum and minimum values and apply derivatives to rates of change problems.</li> </ul>
6	Calculus	Pre-SAC Review
7-8	Calculus	UNIT 3 FN & CALC SAC: 7 lessons, 350 mins = 5 hrs, 50 mins A function and calculus-based investigation of 4–6 hours over 1–2 weeks.
9-10	Calculus	<ul> <li>Integration: 11A – 11E</li> <li>Integrate polynomial functions, exponential functions and circular functions. eg: (ax + b)<sup>r</sup>, e<sup>kx</sup></li> <li>Estimate the area under the graph of a function.</li> </ul>
Term 3 1-2	Calculus	<ul> <li>Applications of Integration: 11F – 11K</li> <li>Integrate by Recognition</li> <li>Use the Fundamental Theorem of Calculus to determine definite integrals and find the exact areas above and below the x-axis and between two curves.</li> </ul>
3	Probability and Statistics	Discrete Random Variables And Their Probability Distributions:  13A–13D  Review the basic concepts of probability including conditional probability.  Define discrete random variables and their probability distributions  Calculate and interpret expected value (mean), variance and standard deviation for a discrete random variable.  Understand that for many random variables approximately 95% of the distribution is within two standard deviations of the mean.
4	Probability and Statistics	<ul> <li>The Binomial Distribution (Bernouilli Trials): 14A – 14D</li> <li>Finding the Sample Size, Proofs for the Expectation and Variance</li> <li>Define a Bernoulli sequence and review the binomial probability distribution.</li> <li>Interpret graphical skewing for different values of the binomial distribution parameters.</li> <li>Calculate and interpret the mean, variance and standard deviation for the binomial probability distribution.</li> <li>Use the binomial probability distribution to solve problems.</li> <li>Find the sample size and proofs for the expectation and variance</li> </ul>

5	Probability	Pre-SAC Review
	and Statistics	
6	Probability	UNIT 4 'APPLICATIONS OF DIFFERENTIATION'
	and Statistics	MODELLING OR PROBLEM SOLVING SAC:
		3 lessons:150 mins = 2.5 hours
		The modelling or problem-solving tasks are 2–3 hours each, over 1 week.
7	Probability	Continuous Random Variables and Their Probability Distributions:
	and Statistics	15A – 15E
		<ul> <li>Introduce continuous random variables and investigate probability density functions.</li> </ul>
		<ul> <li>Relate the probability for an interval to an area under the graph of a probability density function.</li> </ul>
		Use calculus and technology to find probabilities for intervals from a
		probability density function.
		Calculate and interpret the expectation (mean), median, variance and
		standard deviation for a continuous random variable.
8	Probability	The Normal Distribution: 16A-16E
	and Statistics	Understand the family of normal distributions as transformations of the
	and Statistics	standard normal distribution, apply standardisation and the 68-95-99.7%
		Rule
		Investigate the effect of changing the values of the parameters on the      The parameters on the parameters of the
		graph of the probability density function.
		Determine normal probabilities and recognise the mean, median,
		variance and standard deviation of a normal distribution.
		Use procedures and technology to determine probabilities and solve
_		problems and the Normal Approximation to the Binomial Distribution
9	Probability	Sampling and Estimation: 17A- 17E
	and Statistics	Understand random samples and how they are obtained, population
		proportion and sample proportion.
		Investigate the sampling distribution of the sample proportion both
		exactly (for small samples) and through simulation.
		<ul> <li>Approximate the sampling distribution of the sample proportion.</li> </ul>
		Use the sample proportion as a point estimate of the population
		proportion and find confidence intervals for the population proportion,
		the margin of error, and illustrate how this varies both with level of
		confidence and with sample size.
10	Probability	UNIT 4 'PROBABILITY & STATISTICS'
	and Statistics	MODELLING OR PROBLEM SOLVING SAC:
		3 lessons: 150 mins = 2.5 hours
		The modelling or problem-solving tasks are 2–3 hours each, over 1 week.
Term 4	AOS 1, 2, 3 and 4	REVISION AND EXAM PRACTICE
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