## Subject: VCE (Mathematical Methods)

## Unit: 3

| Week | Area of Study | Learning Focus |
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| Term 4 | Headstart | Functions and Relations: 1A-1H, 2A, 2B <br> - Investigate concepts of relations and functions, domain, implied (maximal) domain, restrictions and range. <br> - Investigate and sketch graphs for odd and even functions, one-to-one and inverse functions, sums and products and addition of ordinates. <br> - Define and use composite functions, strictly increasing and decreasing functions and power functions and their graphs. <br> - Apply a knowledge of functions to solve problems. |
| $\begin{gathered} \text { Term } 1 \\ 1-3 \end{gathered}$ | Functions and Graphs <br> Algebra | Coordinate Geometry and Matrices: 2C - 2G, 3A, 3B. <br> - Solving linear and literal equations, simultaneous linear equations with two or more variables and interpret the geometry <br> - Find the distance between two points, midpoint of a line segment and gradient of a straight line. <br> - Recognise different forms of the equation of a straight line and use matrices. <br> - Apply a knowledge of linear functions to solve problems. |
| 4-5 | Functions and Graphs <br> Algebra | Transformations: 3C-3I <br> - Use notation for translations, reflections in an axis and dilations from an axis and determine sequences of transformations given an original and image equation, and use them to sketch graphs. <br> - Consider transformations of power functions. <br> - Determine function rules from transformations and graphs. <br> - Use matrices to define transformations and determine images. |
| 6 | Functions and Graphs <br> Algebra | Polynomial Functions: 3J, 4A -4F <br> - Revise properties of quadratic functions and consider properties of cubic functions and polynomials of higher degree. <br> - Add, subtract, multiply and divide polynomials, equate coefficients and use sign diagrams. <br> - Use the language of polynomials, the remainder theorem, factor theorem and the rational-root theorem and identify the linear factors of cubic and quartic polynomials. <br> - Determine the rules for given polynomial graphs and apply polynomial functions to problem solving. |
| 7 | Functions and Graphs <br> Algebra | Exponential and Logarithmic Functions: 4G-4H, 5A - 5E <br> - Graph exponential and logarithmic functions and their transformations. <br> - Revise the index and logarithm laws and solve exponential and logarithmic equations. <br> - Determine rules for graphing exponential and logarithmic functions and find their inverses. <br> - Apply exponential functions to modelling growth and decay. |
| 8-9 | Functions and Graphs <br> Algebra | Circular Functions: 5F-5I, 6A-6C Circular Function Graphing: 6D-6L <br> - Define the sine, cosine and tangent circular functions, explore their symmetry properties, apply the Pythagorean Identity, find exact values and sketch graphs of circular functions and their transformations. <br> - Measure angles in degrees and radians, solve equations and apply circular functions in modelling periodic motion. <br> - Use addition of ordinates, determine rules for graphing and find general solutions of trigonometric equations <br> - Apply circular functions to problem solving |
| 10 | Functions and Graphs <br> Algebra | Further Functions: 7A-7E <br> - Graph power functions with rational non-integer index. |


|  |  | - Revisit sums, differences and products of functions, addition of ordinates, one-to-one functions, strictly increasing and decreasing functions, odd functions and even functions, composite functions, inverse functions and transformations of functions. <br> - Use functional equations to describe properties of functions. <br> - Use parameters to describe families of functions. |
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|  | Calculus | Differentiation: 9A-9C <br> - Understand limits, the definition of differentiation and the notation for the derivative of a polynomial function. <br> - Find the gradient of a tangent to the graph of a polynomial function by calculating its derivative. |
| $\begin{gathered} \text { Term } 2 \\ 1-3 \end{gathered}$ | Calculus | Differentiation continued: 9D-9M <br> - Understand and use the chain, product and quotient rules. . <br> - Differentiate rational powers, exponential, natural logarithmic and circular functions. <br> - Deduce the graph of the derivative from the graph of a function and vice versa, determine continuity and differentiability |
| 4-5 | Calculus | Applications of Differentiation: 10A - 10G <br> - Find the equations of the tangent and the normal at a given point. <br> - Find stationary points and state their nature. <br> - Use differentiation techniques to sketch graphs and show families of functions <br> - Solve maximum and minimum problems, determine absolute maximum and minimum values and apply derivatives to rates of change problems. |
| 6 | Calculus | Pre-SAC Review |
| 7-8 | Calculus | UNIT 3 FN \& CALC SAC: 7 lessons, 350 mins $=5 \mathrm{hrs}, 50 \mathrm{mins}$ A function and calculus-based investigation of 4-6 hours over 1-2 weeks. |
| 9-10 | Calculus | Integration: 11A-11E <br> - Integrate polynomial functions, exponential functions and circular functions. eg: $(a x+b)^{r}, e^{k x}$ <br> - Estimate the area under the graph of a function. |
| $\begin{gathered} \text { Term } 3 \\ 1-2 \end{gathered}$ | Calculus | Applications of Integration: 11F-11K <br> - Integrate by Recognition <br> - Use the Fundamental Theorem of Calculus to determine definite integrals and find the exact areas above and below the $x$-axis and between two curves. |
| 3 | Probability and Statistics | Discrete Random Variables And Their Probability Distributions: 13A-13D <br> - Review the basic concepts of probability including conditional probability. <br> - Define discrete random variables and their probability distributions <br> - Calculate and interpret expected value (mean), variance and standard deviation for a discrete random variable. <br> - Understand that for many random variables approximately $95 \%$ of the distribution is within two standard deviations of the mean. |
| 4 | Probability and Statistics | The Binomial Distribution (Bernouilli Trials): 14A - 14D <br> Finding the Sample Size, Proofs for the Expectation and Variance <br> - Define a Bernoulli sequence and review the binomial probability distribution. <br> - Interpret graphical skewing for different values of the binomial distribution parameters. <br> - Calculate and interpret the mean, variance and standard deviation for the binomial probability distribution. <br> - Use the binomial probability distribution to solve problems. <br> - Find the sample size and proofs for the expectation and variance |


| 5 | Probability <br> and Statistics | Pre-SAC Review <br> 6 <br> 7 <br> and Statistics |
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